



HAMBURG, den 6 März 1894.

Erw. Hochwohlgeboren.

Ihre freundlichen Glückwünsche verbunden mit der Überreichung einer Reihe wertvoller Arbeiten, welche Sie der Mathematischen Gesellschaft in Hamburg zu ihrem Jubelfeste übersandt haben das lebhafteste Interesse der Gesellschaft gefunden und spricht dieselbe hiermit ihren verbindlichen Dank aus. Die Gesellschaft freut sich glücklich die Teilnahme so vieler berühmter Gelehrten gefunden zu haben. Genehmigen Sie die Versicherung aufrichtigster Hochschätzung und Dankbarkeit seitens

An
Herrn Professor
Césaro - Palermo.

der Mathematisch. Gesellschaft
in Hamburg.
H. Ern. Flappe
b. t. Schriftführer

$$\int \Phi(p_x, p_y, p_z) ds$$

$$\iiint d^3p d^3q dz =$$

$$= \int \Delta ds$$

$$\begin{matrix} p_x & p_y & p_z \\ q_x & q_y & q_z \\ z_x & z_y & z_z \end{matrix}$$

$$\begin{aligned} & p_x q_y z_z + p_y q_z z_x + p_z q_x z_y - \\ & p_x q_z z_y - p_y q_x z_z - p_z q_y z_x \end{aligned}$$

$$q_x z_x$$

$$q_x (p_z z_y - p_y z_z) + z_x (p_y q_z - p_z q_y)$$

$$\frac{\partial a}{\partial z} (p_z z_y - p_y z_z) + \frac{\partial a}{\partial y} (p_z q_y - p_y q_z)$$

$$\frac{\partial}{\partial z} \left(\frac{\partial p}{\partial z} \frac{\partial z}{\partial y} - \frac{\partial p}{\partial y} \frac{\partial z}{\partial z} \right) + \frac{\partial}{\partial y} \left(\frac{\partial p}{\partial z} \frac{\partial q}{\partial y} - \frac{\partial p}{\partial y} \frac{\partial q}{\partial z} \right)$$

$$\frac{\partial p}{\partial z} \frac{\partial z}{\partial y} + \frac{\partial z}{\partial y} \frac{\partial p}{\partial z} - \frac{\partial p}{\partial y} \frac{\partial z}{\partial z} - \frac{\partial p}{\partial z} \frac{\partial q}{\partial y} - \frac{\partial p}{\partial y} \frac{\partial q}{\partial z} + \frac{\partial p}{\partial z} \frac{\partial q}{\partial y} - \frac{\partial p}{\partial y} \frac{\partial q}{\partial z}$$

δa

$$\delta p_x = \frac{\partial \delta a}{\partial z}$$

$$\delta p_y = \frac{\partial \delta a}{\partial y}$$

$q_x \quad z_2$

$$p_x^2 + q_y^2 + z_2^2 + 2p_x q_y + 2p_x z_2 + 2q_y z_2$$

$$\left(\frac{\partial g}{\partial y} - \frac{\partial h}{\partial z} \right)^2$$

~~$$\left(\frac{\partial f}{\partial x} \right)^2 + \left(\frac{\partial g}{\partial y} \right)^2 + \left(\frac{\partial h}{\partial z} \right)^2 - \frac{\partial g}{\partial y} \frac{\partial h}{\partial z} - \frac{\partial h}{\partial z} \frac{\partial g}{\partial y} - \frac{\partial f}{\partial x} \frac{\partial h}{\partial z} - \frac{\partial f}{\partial x} \frac{\partial g}{\partial y}$$~~

~~$$\left(\frac{\partial f}{\partial x} \right)^2 - \frac{\partial f}{\partial x} \left(\frac{\partial g}{\partial y} + \frac{\partial h}{\partial z} \right)$$~~

$$\left(\frac{\partial f}{\partial x} \right)^2 - \frac{\partial f}{\partial x} \left(\frac{\partial g}{\partial y} + \frac{\partial h}{\partial z} \right)$$

$$2 \frac{\partial}{\partial x} \left(\frac{\partial f}{\partial x} \right) - 2 \frac{\partial f}{\partial x} \left(\frac{\partial g}{\partial y} + \frac{\partial h}{\partial z} \right) = 0$$

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$$\lambda_1 u_1 + \lambda_2 u_2 + \dots + \lambda_n u_n = 0$$

$$\left\{ \begin{array}{l} u_1 = a_{11}x_1 + a_{12}x_2 + \dots + a_{1n}x_n \\ u_2 = a_{21}x_1 + a_{22}x_2 + \dots + a_{2n}x_n \\ \dots \\ u_m = a_{m1}x_1 + a_{m2}x_2 + \dots + a_{mn}x_n \end{array} \right.$$

$$\lambda_1 u_1 + \dots + \lambda_m u_m = 0$$

$$\lambda_1 a_{11} + \lambda_2 a_{21} + \dots + \lambda_m a_{m1} = 0$$

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n equations m unknowns

$p < m$

x_1
 \vdots

$x = 1$

$r = 2$

$r = 2$

$$\left(\begin{array}{cccc|ccc} 1 & 0 & 1 & 1 & 1 & 0 & 0 \\ 0 & 1 & 1 & 1 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 1 & 0 \\ 0 & 0 & 0 & 0 & 1 & 1 & 0 \\ 0 & 0 & 0 & 0 & 1 & 1 & 0 \end{array} \right) = \left(\begin{array}{ccc} 0 & 0 & 0 \end{array} \right)$$