

$$\operatorname{sh} \frac{x}{a} = \frac{1}{a} (e^{\frac{x}{a}} - e^{-\frac{x}{a}})$$

$$\operatorname{ch}^2 - \operatorname{sh}^2 = 1$$

$$\sin \frac{z}{a} = \operatorname{sh} \frac{x}{a} \operatorname{sh} \frac{y}{a}$$

$$\operatorname{sh} \frac{x}{a} = \operatorname{tg}(u+v)$$

$$\operatorname{sh} \frac{y}{a} = \operatorname{tg}(u-v)$$

$$\frac{dx}{a} = a \frac{du+dv}{\cos^2(u+v)}$$

$$\frac{dy}{a} = a \frac{du-dv}{\cos^2(u-v)}$$

~~$$\frac{p \cos \frac{z}{a}}{a} = \frac{1}{a} \operatorname{sh} \frac{x}{a}$$~~

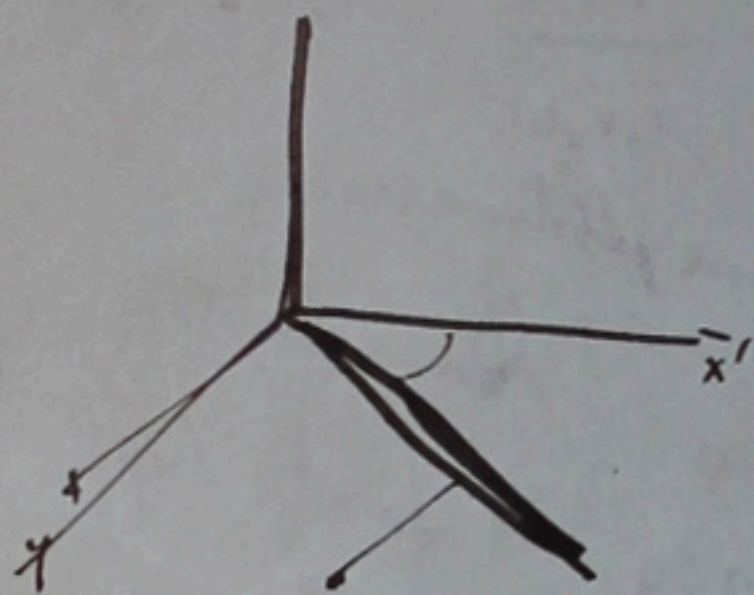
~~$$\frac{p \cos \frac{y}{a}}{a} = \frac{1}{a} \operatorname{ch} \frac{x}{a} \frac{du+dv}{\cos^2(u+v)} \cdot \frac{\operatorname{tg}(u-v)}{\sqrt{1-\operatorname{tg}^2(u+v)\operatorname{tg}^2(u-v)}}$$~~

$$p = \frac{(du+dv) \operatorname{tg}(u-v)}{\cos^2(u+v) \sqrt{\cos 2u \cos 2v}}$$

~~$$\cos(u+v)\cos(u-v) =$$~~

~~$$\frac{q}{a} \cos \frac{z}{a} = \operatorname{sh} \frac{x}{a} \cdot \frac{dy}{a}$$~~

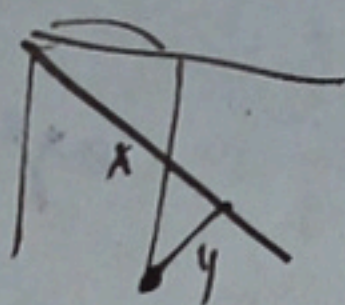
~~$$\frac{(du-dv) \sqrt{1-\operatorname{tg}^2(u-v)}}{\cos(u-v) \sqrt{1-\operatorname{tg}^2(u+v)\operatorname{tg}^2(u-v)}} \sin(u+v) \cdot \cos(u+v)$$~~



$$q = \frac{\sin(u+v) \cdot (du-dv)}{\cos(u-v) \sqrt{\cos 2u \cos 2v}}$$

$$\sin \frac{z}{a} = \operatorname{sh} \frac{x'}{a} \operatorname{sh} \frac{y'}{a}$$

$$= \operatorname{sh} \frac{x+y}{a\sqrt{2}} \operatorname{sh} \frac{x-y}{a\sqrt{2}}$$



$$x' = \frac{x-y}{\sqrt{2}}$$

$$y' = \frac{x+y}{\sqrt{2}}$$

$$\frac{1}{2}(e^\alpha - e^{-\alpha}) \cdot \frac{1}{2}(e^\beta - e^{-\beta})$$

$$\operatorname{sh}(\alpha+\beta) = \frac{1}{2}(e^{\alpha+\beta} - e^{-\alpha-\beta})$$

$$\operatorname{sh} x = \frac{1}{2}(e^x - e^{-x})$$

~~$$\operatorname{sh} ix = i \operatorname{sen} x$$~~

~~$$\operatorname{sh} x = i \operatorname{sen} ix$$~~

$$\operatorname{ch} x = \frac{1}{2}(e^x + e^{-x})$$

~~$$\operatorname{cos} ix = \frac{1}{2}(e^x + e^{-x})$$~~

~~$$\operatorname{sh} \frac{z}{a} = \left(\operatorname{sh} \frac{x}{a\sqrt{2}} \operatorname{ch} \frac{y}{a\sqrt{2}} \right) - \left(\operatorname{sh} \frac{y}{a\sqrt{2}} \operatorname{ch} \frac{x}{a\sqrt{2}} \right)$$~~

$$\operatorname{sh}(\alpha+i\beta) = -i \operatorname{sen}(\alpha+i\beta)$$

$$= -i \operatorname{sen} \alpha \operatorname{cos} \beta - i \operatorname{sen} \alpha \operatorname{sen} \beta$$

$$= \operatorname{sh} \alpha \operatorname{cos} \beta - \operatorname{sh} \beta \operatorname{ch} \alpha$$

$$\sin \frac{z}{a} = \operatorname{sh}^2 \frac{x}{a\sqrt{2}} \left[1 + \operatorname{sh} \frac{y}{a\sqrt{2}} \right] - \operatorname{sh}^2 \frac{y}{a\sqrt{2}} \left[1 + \operatorname{sh} \frac{x}{a\sqrt{2}} \right]$$